Impedance transmission conditions for thin conducting sheets

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Thin shielding sheets in low frequency electromagnetic devices are difficult to model within the eddy current model when using standard FE discretisations. This is due to the smallness of the layer which would lead to a huge number of elements in and around the sheet. The sheets are therefore replaced by impedance transmission conditions [1–3], similarly to impedance boundary conditions for thin coatings. The previous conditions turn out to be of first order in the sheet thickness [4]. For the case of smooth sheets, we will present frameworks to derive impedance transmission conditions to any order [5, 6] and show results up to third order. We will discuss the stability, robustness w.r.t. to frequency (or equivalently skin depth) of the impedance boundary conditions as well as their use in variational formulations like in a FE discretisation. Numerical results will verify the theoretical findings.



Figure 1: Magnetic fields around two live wires shielded by an ellipsoidal thin conducting sheet.

References

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